

Calculus Surds Practice #1

Simplify fully:

1. $5\sqrt{20} + 4\sqrt{45}$

2. $2\sqrt{10} \times 3\sqrt{20}$

3. $\frac{\sqrt{75}}{\sqrt{48}}$

4. $\frac{\sqrt{81}}{\sqrt{27}}$

5. $\frac{\sqrt{8x^3}}{4\sqrt{2x}}$

Expand and simplify fully:

6. $\sqrt{28}(3 + 4\sqrt{7})$

7. $(3 + \sqrt{7})(3 - \sqrt{7})$

8. $(\sqrt{2} + \sqrt{3})(\sqrt{8} + \sqrt{12})$

9. $(x + \sqrt{8})(x - \sqrt{2})$

10. $(x - \sqrt{5})(x - \sqrt{20})$

Rationalise the denominator, then simplify fully:

11. $\frac{3\sqrt{3}}{\sqrt{2}}$

12. $\frac{\sqrt{35}}{3\sqrt{5}}$

13. $\frac{\sqrt{7}}{4 + \sqrt{7}}$

14. $\frac{4 + \sqrt{18}}{3 - \sqrt{2}}$

15. $\frac{2 + \sqrt{5}}{2 - \sqrt{5}}$

Prove that:

16. $\frac{5(a - 3\sqrt{a})}{a - 9} = \frac{5\sqrt{a}}{3 + \sqrt{a}}$

Answers: Calculus Surds Practice #1

Simplify fully:

$$\begin{array}{llll}
 1. & 5\sqrt{20} + 4\sqrt{45} & = 5\sqrt{4}\sqrt{5} + 4\sqrt{9}\sqrt{5} & = 10\sqrt{5} + 12\sqrt{5} \\
 & & & = 22\sqrt{5} \\
 \\
 2. & 2\sqrt{10} \times 3\sqrt{20} & = 6\sqrt{200} & = 6\sqrt{100}\sqrt{2} \\
 & & & = 60\sqrt{2} \\
 \\
 3. & \frac{\sqrt{75}}{\sqrt{48}} & = \frac{\sqrt{25}\sqrt{3}}{\sqrt{16}\sqrt{3}} & = \frac{5\sqrt{3}}{4\sqrt{3}} \\
 & & & = \frac{5}{4} \\
 \\
 4. & \frac{\sqrt{81}}{\sqrt{27}} & = \frac{3 \times 3}{3\sqrt{3}} & = \frac{3\sqrt{3}\sqrt{3}}{3\sqrt{3}} \\
 & & & = \sqrt{3} \\
 \\
 5. & \frac{\sqrt{8x^3}}{4\sqrt{2x}} & = \frac{\sqrt{4}\sqrt{x^2}\sqrt{2x}}{4\sqrt{2x}} & = \frac{2x\sqrt{2x}}{4\sqrt{2x}} \\
 & & & = \frac{x}{2}
 \end{array}$$

Expand and simplify fully:

$$\begin{array}{llll}
 6. & \sqrt{28}(3 + 4\sqrt{7}) & = 3\sqrt{28} + 4\sqrt{196} & = 6\sqrt{7} + 56 \\
 \\
 7. & (3 + \sqrt{7})(3 - \sqrt{7}) & = 9 - 3\sqrt{7} + 3\sqrt{7} - 7 & = 2 \\
 \\
 8. & (\sqrt{2} + \sqrt{3})(\sqrt{8} + \sqrt{12}) & = \sqrt{16} + \sqrt{24} + \sqrt{24} + \sqrt{36} & = 10 + 4\sqrt{6} \\
 \\
 9. & (x + \sqrt{8})(x - \sqrt{2}) & = x^2 - \sqrt{2}x + \sqrt{8}x - \sqrt{16} & = x^2 + \sqrt{2}x - 4 \\
 \\
 10. & (x - \sqrt{5})(x - \sqrt{20}) & = x^2 - \sqrt{20}x - \sqrt{5}x + \sqrt{100} & = x^2 - 3\sqrt{5}x + 10
 \end{array}$$

Rationalise the denominator, then simplify fully:

$$\begin{array}{llll}
 11. & \frac{3\sqrt{3}}{\sqrt{2}} & = \frac{3\sqrt{3}\sqrt{2}}{\sqrt{2}\sqrt{2}} & = \frac{3\sqrt{6}}{2} \\
 & & & = \frac{3\sqrt{6}}{2} \\
 \\
 12. & \frac{\sqrt{35}}{3\sqrt{5}} & = \frac{\sqrt{35}\sqrt{5}}{3\sqrt{5}\sqrt{5}} & = \frac{5\sqrt{7}}{15} \\
 & & & = \frac{\sqrt{7}}{3} \\
 \\
 13. & \frac{\sqrt{7}}{4 + \sqrt{7}} & = \frac{\sqrt{7}(4 - \sqrt{7})}{(4 + \sqrt{7})(4 - \sqrt{7})} & = \frac{4\sqrt{7} - \sqrt{49}}{16 - 7} \\
 & & & = \frac{4\sqrt{7} - 7}{9} \\
 \\
 14. & \frac{4 + \sqrt{18}}{3 - \sqrt{2}} & = \frac{(4 + \sqrt{18})(3 + \sqrt{2})}{(3 - \sqrt{2})(3 + \sqrt{2})} & = \frac{12 + 4\sqrt{2} + 3\sqrt{18} + \sqrt{36}}{9 - 2} \\
 & & & = \frac{18 + 13\sqrt{2}}{7} \\
 \\
 15. & \frac{2 + \sqrt{5}}{2 - \sqrt{5}} & = \frac{(2 + \sqrt{5})(2 + \sqrt{5})}{(2 - \sqrt{5})(2 + \sqrt{5})} & = \frac{4 + 2\sqrt{5} + 2\sqrt{5} + \sqrt{25}}{4 - 5} \\
 & & & = -9 - 4\sqrt{5}
 \end{array}$$

Proof:

$$\begin{array}{ll}
 16. & \text{much easier in reverse: } \frac{5\sqrt{a}}{3 + \sqrt{a}} \\
 & = \frac{5\sqrt{a}(3 - \sqrt{a})}{(3 + \sqrt{a})(3 - \sqrt{a})} \\
 & = \frac{15\sqrt{a} - 5\sqrt{a}\sqrt{a}}{9 - a} \\
 & = \frac{15\sqrt{a} - 5a}{9 - a} \\
 & = \frac{5(a - 3\sqrt{a})}{a - 9}
 \end{array}$$